4.1 Completed Notes

4.1: Divisibility

Definition: For two whole numbers a and b, $b \neq 0$, we say \underline{b} divides \underline{a} , written as $b \mid a$, if $a \div b$ is a whole number. Other ways to say this are "a is divisible by b", "b is a divisor of a", "a is a multiple of b", and "b is a factor of a".

Divisibility Rules: Let *n* be a whole number.

 $2 \mid n$ if and only if n ends in an even number.

 $3 \mid n$ if and only if the sum of the digits of n is divisible by 3. Example: Show $3 \mid 5352$.

 $4 \mid n$ if and only if 4 divides the last 2 digits of n. Example: Show $4 \mid 1880$.

 $5 \mid n$ if and only if n ends in either 0 or 5.

Divisibility Rules: Let *n* be a whole number.

 $6 \mid n$ if and only if $2 \mid n$ and $3 \mid n$.

For 7, form a new number k by taking off the last digit of n and subtracting its double from the result. Then $7 \mid n$ if and only if $7 \mid k$. Example: Show that $7 \mid 3654$.

$$365-2.4=357$$
 $7|2|, 50 7|357$
 $35-2.7=21$ Thus, $7|3654$

 $8 \mid n$ if and only if 8 divides the last 3 digits of n.

 $9 \mid n$ if and only if the sum of the digits of n is divisible by 9.

 $10 \mid n$ if and only if n ends in 0.

For 11, we form a new number k by adding then subtracting the digits of n. It is important that we consider the sign of the first digit as part of this addition and subtraction. Then $11 \mid n$ if and only if $11 \mid k$. Example: Show that $11 \mid 1485$.

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Example: Determine which of the numbers 2 through 11 divide 1680. Justify

$$(1) \stackrel{\dagger}{|} \stackrel{\dagger}{|}$$

Example: Determine which of the numbers 2 through 11 divide 1680. Justify each of your tests.

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Example: Determine which of the numbers 2 through 11 divide 13860. Justify each of your tests.

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$$(1) \frac{13860}{13860} \longrightarrow |-3+8-6+0=0$$

$$|1|_{0_{1}} = |-3+8-6+0=0$$